

Name:

Solutions / Answers

Unit 1.8 (the only material from unit 1.8 included in Wednesday's quiz is the graphing of parabola)

1. Graph the parabola with quadratic equation

$$f(x) = 7 - x^2$$

$$f(x) = -x^2 + 0x + 7$$

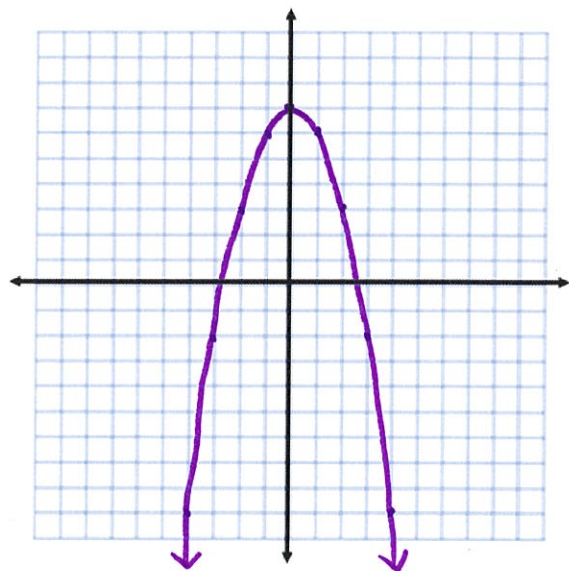
$$a = -1 \quad b = 0 \quad c = 7$$

$$\text{axis } x = \frac{-0}{2(-1)} = 0$$

$$f(0) = 7 - (0)^2 = 7$$

$$V(0, 7)$$

Pattern: 1, 3, 5, 7, 9 but down



2. Graph the parabola with quadratic equation

$$f(x) = 2x^2 - 12x + 11$$

$$\text{axis } x = \frac{-(-12)}{2(2)} = \frac{12}{4} = 3$$

$$f(3) = 2(3)^2 - 12(3) + 11$$

$$= 2(9) - 36 + 11$$

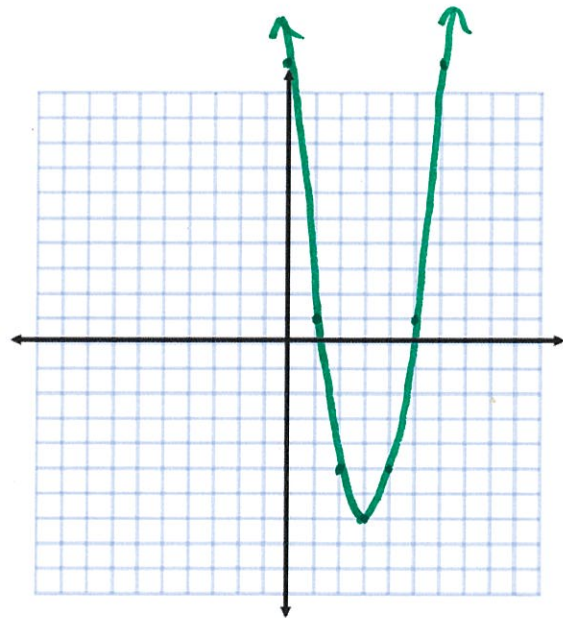
$$= 18 - 36 + 11$$

$$= -18 + 11$$

$$= -7$$

$$V(3, -7)$$

Pattern: 2, 6, 10, ...

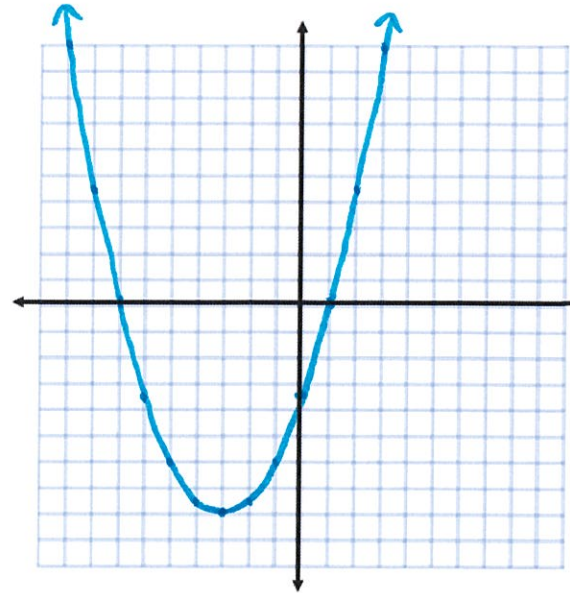


3. Graph the parabola with quadratic equation

$$f(x) = \frac{1}{2}(x+3)^2 - 8$$

$$V(-3, -8)$$

Pattern: $\frac{1}{2}, 1\frac{1}{2}, 2\frac{1}{2}, 3\frac{1}{2}, 4\frac{1}{2}, 5\frac{1}{2}$



4. Graph the parabola with quadratic equation

$$f(x) = -(x-1)(x-7)$$

x-intercepts are (1,0) & (7,0)

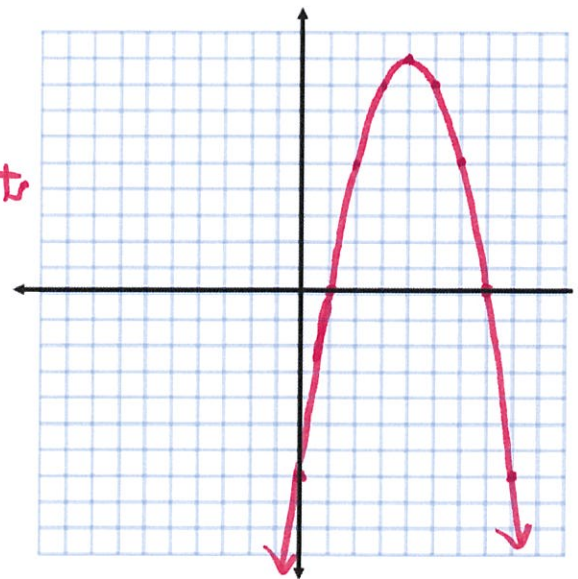
axis is at midpoint of x-intercepts

$$\text{axis } x = \frac{1+7}{2} = \frac{8}{2} = 4$$

$$\begin{aligned} f(4) &= -(4-1)(4-7) \\ &= -(3)(-3) \\ &= 9 \end{aligned}$$

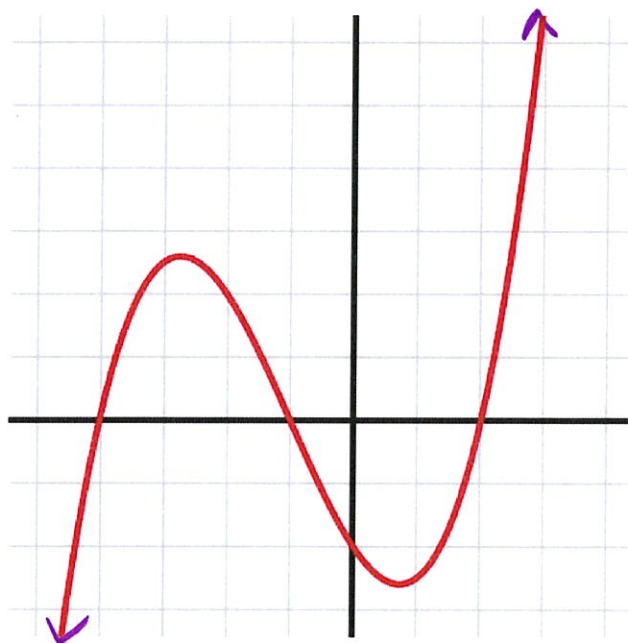
$$V(4, 9)$$

Pattern: 1, 3, 5, 7, ... but down



Unit 1.7 Material

5. Shown is the graph of $y = g(x)$



Domain: $(-\infty, \infty)$	Range: $(-\infty, \infty)$
Increasing on what interval? $(-\infty, -2.75) \cup (0.75, \infty)$	Decreasing on what interval? $(-2.75, 0.75)$
Maximum Value: $y = \text{None}$	Minimum Value: $y = \text{None}$
Concave up: $(-1, \infty)$	Concave Down: $(-\infty, -1)$
$g(x) > 0$ $(-4, -1) \cup (2, \infty)$	$g(x) \leq 0$ $(-\infty, -4] \cup [-1, 2]$
Coordinates of the x-intercept(s): $(x, y) = (-4, 0); (-1, 0); (2, 0)$	Coordinates of the y-intercept: $(x, y) = (0, -2)$
End Behavior as $x \rightarrow -\infty$ $y \rightarrow -\infty$	End Behavior as $x \rightarrow \infty$ $y \rightarrow \infty$

Unit 1.8 Material

Given the two functions $f(x) = 6 - x$ and $g(x) = 3x + 10$, evaluate each expression:

1. $(f - g)(x)$ or $f(x) - g(x)$

$$\begin{aligned} 6 - x - (3x + 10) \\ 6 - x - 3x - 10 \\ -4x - 4 \end{aligned}$$

2. $\left(\frac{g}{f}\right)(2)$ or $\frac{g(2)}{f(2)}$ $= \frac{3(2) + 10}{6 - 2} = \frac{6 + 10}{4} = \frac{16}{4} = 4$

3. $(f \cdot g)(x)$ or $f(x) \cdot g(x)$ $= (6 - x)(3x + 10)$
 $= 18x + 60 - 3x^2 - 10x$
 $= -3x^2 + 8x + 60$

4. $(g \circ f)(x)$ or $g(f(x))$ $= g(6 - x) = 3(6 - x) + 10$
 $= 18 - 3x + 10$
 $= 28 - 3x$

Given the two functions $f(x) = 2x^2 - 6$ and $g(x) = \sqrt{x+5}$, Then evaluate each expression:

$$\begin{aligned} 5. (f \circ g)(x) \text{ or } f(g(x)) &= f(\sqrt{x+5}) = 2(\sqrt{x+5})^2 - 6 \\ &= 2(x+5) - 6 \\ &= 2x + 10 - 6 \\ &= 2x + 4 \end{aligned}$$

$$\begin{aligned} 6. (g \circ f)(x) \text{ or } g(f(x)) &= g(2x^2 - 6) = \sqrt{2x^2 - 6 + 5} \\ &= \sqrt{2x^2 - 1} \end{aligned}$$

$$\begin{aligned} 7. (f \circ g)(11) \text{ or } f(g(11)) &= f(\sqrt{11+5}) = f(\sqrt{16}) \\ &= f(4) \\ &= 2(4)^2 - 6 \\ &= 2(16) - 6 \\ &= 32 - 6 \\ &= 26 \end{aligned}$$

$$\begin{aligned} 8. (g \circ f)(-5) \text{ or } g(f(-5)) &= g(2(-5)^2 - 6) = g(2(25) - 6) \\ &= g(50 - 6) \\ &= g(44) \\ &= \sqrt{44 + 5} \\ &= \sqrt{49} \\ &= 7 \end{aligned}$$